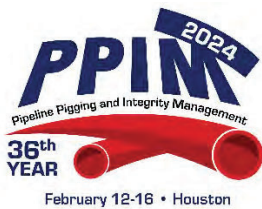


# Pipeline Stacked Crack Interaction Burst Pressure Analysis Using 3-D Crack Meshes

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## 1. Abstract

Accurate evaluation of the remaining strength of crack-like flaws identified via pipeline inline inspection or in-ditch non-destructive examination (NDE) is critical to ensuring continued safe operation of liquid and gas transmission pipelines. Modern pipeline ILI tools have sufficient resolution to detect longitudinally overlapping crack-like flaws that exist in the same radial plane, referred to as stacked cracks. Depending upon the crack sizes and pressure loading, stacked cracks can interact to reduce burst pressure below that of the individual stacked cracks.

Closely located cracks are often evaluated using interaction criteria, such as those provided by API 579-1/ASME FFS-1 Fitness-for-Service Part 9 [1], which specify how and when multiple nearby cracks can be combined into a single crack for the purpose of an integrity assessment. When applied to stacked cracks, the interaction criteria can often lead to a more urgent response from the pipeline operator.

Here, improved interaction criteria were developed for stacked cracks found in pipelines based on the results of elastic-plastic finite element analysis models of multiple combinations of stacked crack sizes and orientations, pipe material properties, and operating stress. These improved interaction criteria for pipelines provide an easy-to-apply methodology to analyze stacked cracks that reduces the excess conservatism associated with legacy methods.

## 2. Introduction

Assessment of crack-like anomalies in pipelines is necessary to a comprehensive pipeline integrity program. Crack assessment models enable pipeline operators to estimate burst pressures associated with cracks of a given dimension in a pipe of given properties and geometry; however, these models typically assume a singular crack in isolation; i.e., not interacting with other nearby cracks.

Some guidance exists on how to assess whether nearby cracks are expected to interact, as well as how to approach the assessment of such a multi-crack system. The widely adopted CorLAST<sup>TM</sup> crack burst pressure model [2] can be used to iteratively evaluate different combinations of profiles from cracks in the same radial orientation (i.e., internal or external) and in close axial proximity to yield either an equivalent crack or the conclusion that evaluating the involved cracks in isolation is a conservative approach. Industry-recommended standards, such as API 579-1/ASME FFS-1 Fitness-for-Service [1] (API 579), provide guidance on combining cracks that are in the same circumferential plane into a single equivalent geometry based on axial and radial separation distances Figure 1. In these cases, it is assumed that assessing the single equivalent crack results in a conservative burst pressure compared to the multi-crack system.

However, both approaches have limitations. Using CorLAST<sup>TM</sup> to combine cracks is only applicable to same-sided, surface-breaking cracks; i.e., both cracks must be on the inner diameter (ID) or outer diameter (OD) of the pipe. API 579 provides no insight regarding the degree of conservatism inherent in the recommended equivalent crack configurations. In fact, these interaction criteria can lead to recategorizing cracks as a through-wall crack that requires urgent response from the pipeline operator, which may be an overly conservative approach and lead to unnecessary mitigative actions. Furthermore, like CorLAST<sup>TM</sup>, API 579 provides no explicit guidance on how to approach two surface-breaking cracks on the ID and OD of the pipe that overlap axially (hereafter referred to as “stacked” cracks).

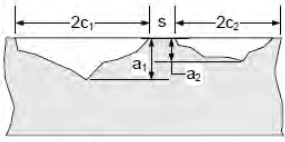
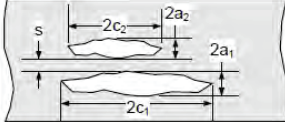
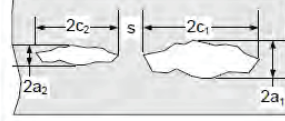
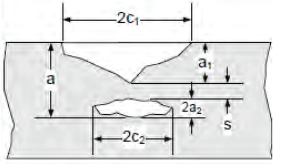
Multiple Crack-Like Flaw Configuration	Criterion For Interaction	Effective Dimensions After Interaction
 <p>Configuration 1</p>	$s \leq \max[0.5a_1, 0.5a_2]$	$2c = 2c_1 + 2c_2 + s$ $a = \max[a_1, a_2]$
 <p>Configuration 2</p>	$s \leq \max[a_1, a_2]$	$2a = 2a_1 + 2a_2 + s$ $2c = \max[2c_1, 2c_2]$
 <p>Configuration 3</p>	$s \leq \max[a_1, a_2]$	$2c = 2c_1 + 2c_2 + s$ $2a = \max[2a_1, 2a_2]$
 <p>Configuration 4</p>	$s \leq \max[0.5a_1, a_2]$	$a = a_1 + 2a_2 + s$ $2c = \max[2c_1, 2c_2]$

Figure 1. Example of API 579 for combining cracks.

With the advent of high-resolution ultrasonic crack detection tools used in ILI and NDE, stacked crack-like defects such as lack-of-fusion (LOF) and hook cracks are being reported with increased frequency in the longitudinal seam of pipes manufactured using low-frequency electric resistance welding (LF-ERW) and flash welding (FW). Considering that these crack-like defects are known to be responsible for a large proportion of past in-service and hydrostatic test failures [3], the ability to understand conditions under which stacked cracks would be expected to interact, and to model the stacked crack system as a single equivalent crack with an associated level of conservatism, is of great use to pipeline operators. Thus, this study developed three-dimensional (3-D) finite element (FE) models of pipes with stacked cracks to explore the behavior of stacked and non-stacked cracks for different combinations of crack depth, pipe geometry, and pipe material properties.

3-D FEA using appropriate crack meshing techniques [4] is an alternative to the API 579 Part 9 criteria. Detailed FEA allows estimation of pipeline burst pressure based on customized combinations of crack geometry, pressure loading, and material properties, which may reduce the conservatism inherent in the Part 9 criteria and allow for analysis of cases not explicitly covered in the guidance. In particular, the case of stacked internal and external surface-breaking cracks, a scenario commonly reported by ILI tools, are not explicitly covered under the Part 9 criteria.

Elastic-plastic FEA of cracks uses concentric rings of brick elements along the crack front to compute the crack front J-integral values over several contours as a function of increasing internal pressure. The crack front brick elements are initially collapsed on one element face with a set of initially

coincident nodes that can displace as loading increases. This behavior helps capture crack front blunting as plasticity develops along the crack front with increasing pressure. The crack meshes use 20-node reduced integration elements. A crack driving force assessment of the stacked cracks then combines the J-integral results with the Level 3 method in API 579 Part 9 Annex 9G.5 to determine burst pressure for a given pipeline steel toughness,  $K_{IC}$ .

Depending on the size of the stacked cracks and the pressure loading level, a high-stress region in the ligament between the stacked cracks can develop. As the plastic zone in the ligament increases, so also does the interaction of the stacked cracks. For closely spaced stacked cracks, the results show crack interaction begins at low pressure. For widely spaced stacked cracks, the results show crack interaction can still occur at higher pressure loads.

### 3. Background

#### 3.1 Pipe Selection

This section details how the pipe dimensions were selected for simulations in this study.

##### 3.1.1 Equal Stacked Cracks

The pipe geometries and material properties explored includes the following configurations:

- NPS 16 grade X52 pipe with 0.25-inch nominal wall thickness (NWT)
- NPS 24 grade X52 pipe with 0.281-inch NWT
- NPS 12 grade X52 pipe with 0.219-inch NWT
- NPS 16 grade X46 pipe with 0.315-inch NWT

It was hypothesized that WT would have a greater influence on crack interaction than pipe diameter given an assumed maximum operating pressure of 72% specified minimum yield strength (SMYS). Therefore, the following geometry configurations were added to identify any trends with respect to WT that could be observed:

- NPS 16 grade X52 pipe with 0.219-inch NWT
- NPS 16 grade X52 pipe with 0.281-inch NWT
- NPS 16 grade X52 pipe with 0.315-inch NWT

Modified interaction criteria were adapted from configuration 4 in Figure 1 to predict when stacked surface-breaking cracks might interact. Given a set of stacked cracks of depth  $a_{ext}$  and  $a_{int}$  with a remaining ligament of

$$s = w.t. - a_{ext} - a_{int} \quad (1)$$

interaction is predicted to occur when

$$s \leq \max(0.5 a_{ext}, 0.5 a_{int}) \quad (2)$$

Assuming equal cracks, the minimum depth required for interaction is 0.4 x WT. Therefore, crack depth levels for the case of equal depths were set to 32.5% and 40% of WT to achieve scenarios below and at depths where interaction would be predicted to occur based on the above equation. Also, given the crack depths and pipe geometries described above, single crack lengths of 2 inches (50.8 mm) and 4 inches (101.3 mm) were chosen for stacked cracks.

### 3.1.2 Unequal Stacked Cracks

For the unequal stacked cracks, only the four pipe geometries initially discussed in Section 3.1.1, were simulated. Because crack depths below 40% through-wall were not predicted to interact based on equation 2, 40% through-wall was used as the lower bound of the deeper of the stacked crack pairs, with 60% through-wall being an upper bound. For the shallower crack of the unequal stacked crack pair, a depth was selected such that the combined depth of both cracks ranged from 70% through-wall up to a depth that interaction was predicted by equation 2. To maintain consistency with the equal depth cases, a crack length of 2 inches (50.8 mm) was maintained here.

## 3.2 Numerical Crack Models

FE techniques have been used to investigate the interaction between stacked surface-breaking cracks compared to single surface-breaking cracks located axially along a pipelines axial plane.

### 3.2.1 Finite Element Models

The image in Figure 2a shows a quarter symmetric cylinder pipe mesh for a 12.75-inch (32.385-cm) OD pipe with a stacked crack located in the upper right portion of the image. A symmetry plane cuts through the pipe's cross-section in the middle of the surface-breaking cracks at the right end of the mesh. Another symmetry plane cuts through the cylinder in the axial direction, resulting in a quarter symmetric model. The pipe's symmetry was leveraged to reduce numerical run times.

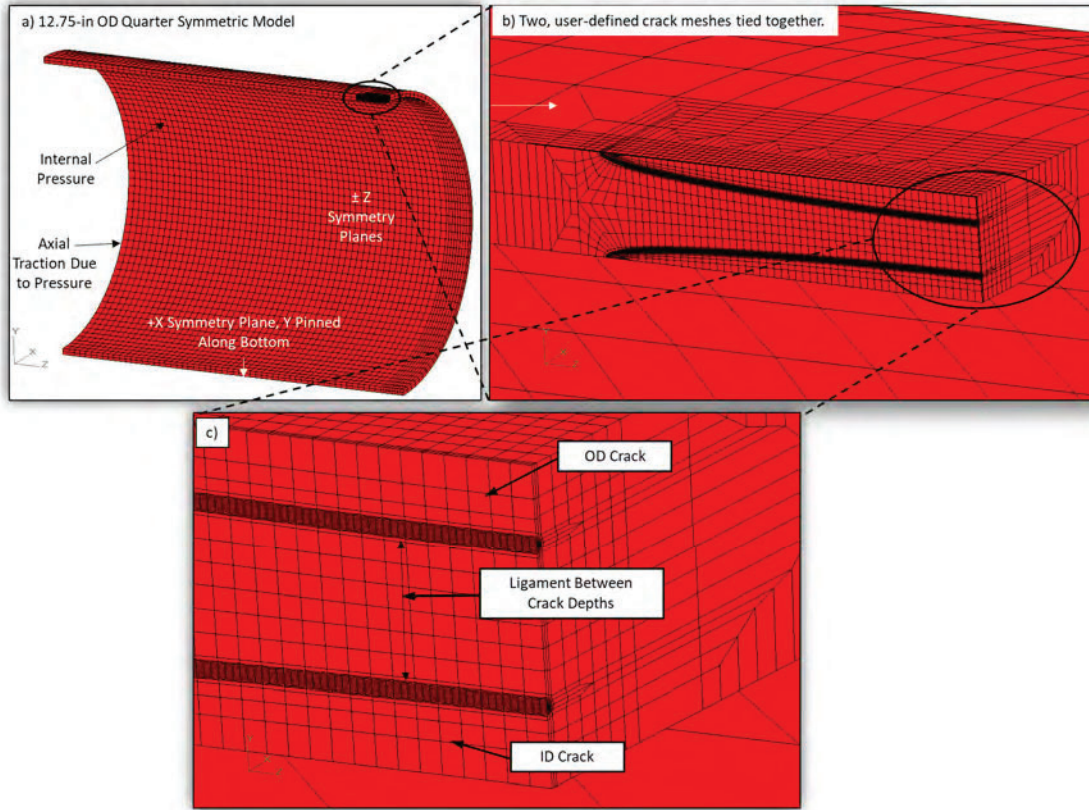
Figure 2b is a close-up of stacked cracks that both measure 2 inches (50.8 mm) in the axial direction—one is an external axial surface-breaking crack and the other is an internal axial surface-breaking crack. The internal and external surface-breaking cracks are the halved, semi-elliptical regions. The highly refined focused crack mesh regions with concentric rings of elements around the crack front are used to compute the crack front J-integral and equivalent stress intensity values along the crack front in the FEA solver [5]. The brick elements in the first contour at the crack front have a collapsed element face with a set of initially coincident nodes at the crack front. The mid-side nodes of the first contour brick elements remain at the element mid-side location for the elastic-plastic analysis. The initially coincident crack front nodes can displace to capture crack front blunting as the applied pressure load increases and yielding occurs near the crack front. In the post-processing, the J-integral results are averaged using contours two through six (first contour omitted) to get the J-integral at each crack front node.

Equivalent stress intensity,  $K$ , is computed from the J-integral values and material property values. API 579 Section 9G.3.5 details an approach for a focused mesh using elastic-plastic analysis, and Equation 9G.1 gives the  $K$  from J equation. These are common approaches and widely accepted methods for calculating J and using it to estimate crack failures [4] [6]. Figure 2c shows a close-up at the crack depth location at the right end of the symmetry plane, where the highly refined mesh around the concentric ring elements is more apparent.

Figure 2b also shows the full length of the semi-elliptical stacked cracks. FEACrack™ [5] was used to build refined crack meshes. The cylinders were first partitioned to allow the external and internal crack depths to fit within two zones. In the case shown in Figure 2b, the partition occurred at the mid-WT because the cracks are equal depths in this example. Although for cases with unequal crack depths, the partition was located to allow the specified crack depths. Once the external and internal



crack meshes were generated in each region, the two mesh regions were combined in a single input file for Abaqus [7] analysis. The two partitioned mesh regions were connected using the tied contact command in FEACrack™ to add the tied contact syntax in the Abaqus input file. Single cracks, which were either surface breaking on the external or internal side were also modelled for comparison with the stacked crack stress intensity. The single crack models did not require partitioning; however, the crack meshes were identical for a direct comparison to the stacked cracks.



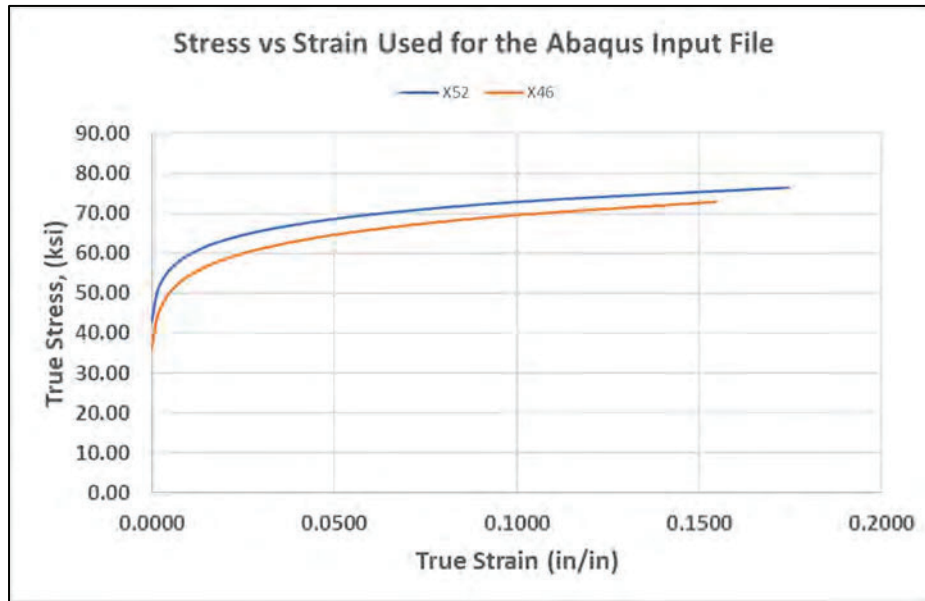
**Figure 2** (a) Quarter symmetric stacked crack model with symmetry constraints highlighted. (b) A closer view of the stacked cracks along with a (c) detailed view of refined crack front elements

Figure 2a highlights the symmetry constraints, internal pressure, and equivalent axial traction stress. The crack face pressure was applied to the internal surface crack partition. Two vintage pipeline materials were explored here—one was X52 grade steel and the other was X46 grade steel. Table 1 summarizes the material properties assumed for the two steel grades explored. A feature in FEACrack™ automatically calculated Ramberg-Osgood curve-fit parameters, as shown in Table 1, which were used to obtain a table of stress-strain values for the Abaqus input file, shown in Figure 3.

The pipe geometries and crack depths explored here are outlined in Table 2, Table 3, and Table 4. Table 2 represents stacked cracks that have equal external ( $a_{ext}$ ) and internal ( $a_{int}$ ) depths. The lengths remained constant at  $2c = 2$  inches (50.8 mm). Table 3 summarizes the scenarios that were explored with differing external ( $a_{ext}$ ) and internal ( $a_{int}$ ) depths. The unequal cracks also maintained a constant length of  $2c = 2$  inches (50.8 mm) for consistency. Table 4 is identical to Table 3 except all the crack lengths are  $2c = 4$  inches (101.6 mm). In addition, all the stacked crack scenarios shown in Table 2 to Table 4 have corresponding single crack models to compare the stress intensity between the stacked cracks and identical single cracks.

**Table 1.** Material properties applied to crack models.

Steel grade	Modulus	Poisson's ratio	Yield strength	Tensile strength	Ramberg-Osgood parameters	
	Ksi (MPa)		Ksi (MPa)	Ksi (MPa)	N	$\alpha$
X52	30,000 (206,842)	0.3	52 (358.5)	66 (455.1)	11.6	1.2
X46	30,000 (206,842)	0.3	46 (317.2)	63 (434.4)	9.4	1.3



**Figure 3.** True stress versus true plastic strain curves used to build the Abaqus input files for X52 and X46 steel material.

## 4. Results

This study first explored stacked cracks where  $a_{ext}$  and  $a_{int}$  are equal (Section 4.1). Next, unequal cracks were explored, where  $a_{int}$  was greater than  $a_{ext}$  (Section 4.2). Because the crack face pressure was applied to the internal surface crack,  $a_{int}$  was the deeper of the two cracks and the more conservative scenario. The final crack sizes explored included doubling the crack length to  $2c = 4$  inch (101.6 mm), which is presented in Section 4.3. Finally, the burst pressures were calculated for all cracks in Section 4.4.

### 4.1 Equal $a_{ext}$ and $a_{int}$ Crack Depths

The scenarios in Table 2 were explored for equal sized stacked cracks. In addition to the stacked cracks shown in Table 2, singular internal crack models were simulated for a direct comparison to identify when stacked cracks begin to interact.

Seven pipe geometries were explored, as outlined in Table 2. Each geometry simulated two equal crack scenarios—one in which the crack depths were 32.5% (65% deep combined) of the WT and



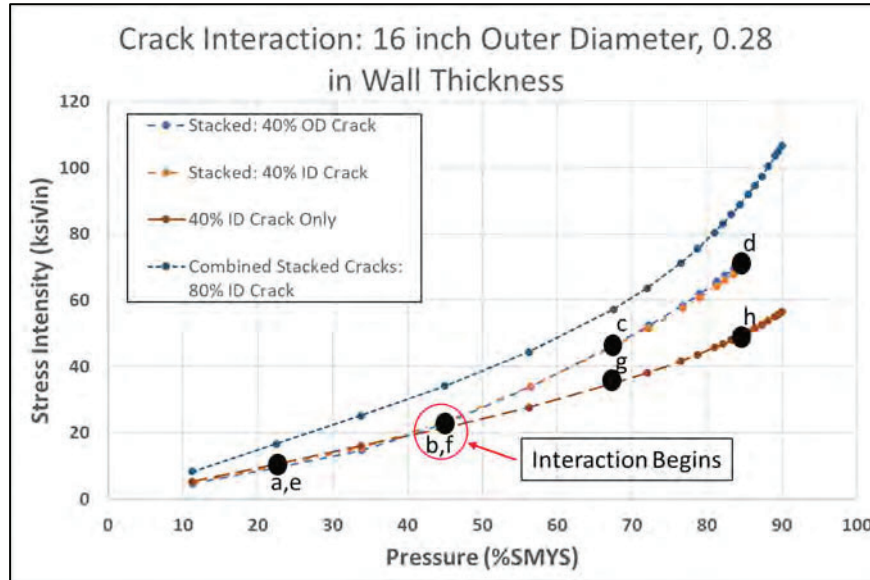
the other with 40% (80% deep combined) deep cracks. Based on the modified API 579 interaction recommendations described in equation 2, all the 32.5% deep cracks failed to meet the current interaction criteria, while the 40% deep cracks meet the interaction criteria. The simulations consistently showed that no interaction was observed when  $a_{ext}$  and  $a_{int}$  both equaled 32.5% of the WT. However, when crack depths were both increased to 40% of the WT, it was observed that the cracks only begin to interact once the internal pressure reached 40% of SMYS.

**Table 2.** Crack models demonstrate the percentage of SMYS where crack interaction starts when the OD and ID crack depths are equal. Crack length was  $2c = 2$  inch (50.8 mm).

Pipe OD Inch (mm)	Pipe WT Inch (mm)	Pipe grade	$a_{ext}$ and $a_{int}$ crack depths	Remaining ligament	Simulated stacked crack interaction begins at?	Meet modified API crack interaction criteria
			% WT	% WT	% SMYS	
12.75 (324)	0.219 (5.56)	X52	32.5	35	No interaction	NO
			40	20	40	YES
16 (406)	0.219 (5.56)	X52	32.5	35	No interaction	NO
			40	20	40	YES
16 (406)	0.25 (6.35)	X52	32.5	35	No interaction	NO
			40	20	40	YES
16 (406)	0.281 (7.14)	X52	32.5	35	No interaction	NO
			40	20	40	YES
16 (406)	0.314 (8.0)	X52	32.5	35	No interaction	NO
			40	20	40	YES
16 (406)	0.314 (8.0)	X46	32.5	35	No interaction	NO
			40	20	40	YES
24 (609)	0.281 (7.14)	X52	32.5	35	No interaction	NO
			40	20	40	YES

Figure 4 plots the stress intensity  $K_j$  (equivalent  $K$  from J-integral results) versus pressure for a pipe geometry in Table 2 that measured 16 inches (406 mm) OD and 0.281 inch (7.14 mm) WT, with crack depths 40% of the WT. Stacked cracks and single ID cracks followed the same stress intensity trend until the pressure reached 40% of SMYS. When the internal pressure reaches 40% of SMYS or greater, the cracks begin to interact, which follows the guidance in equation 2. The interaction points shown throughout this report were estimated based upon visualizing stress-intensity plots at the immediate onset of deviation between the singular ID crack and the stacked ID crack. The simulated pressure steps when interaction occurred were often coarse (10% SMYS between points), which added to the uncertainty in the interaction pressure estimation.

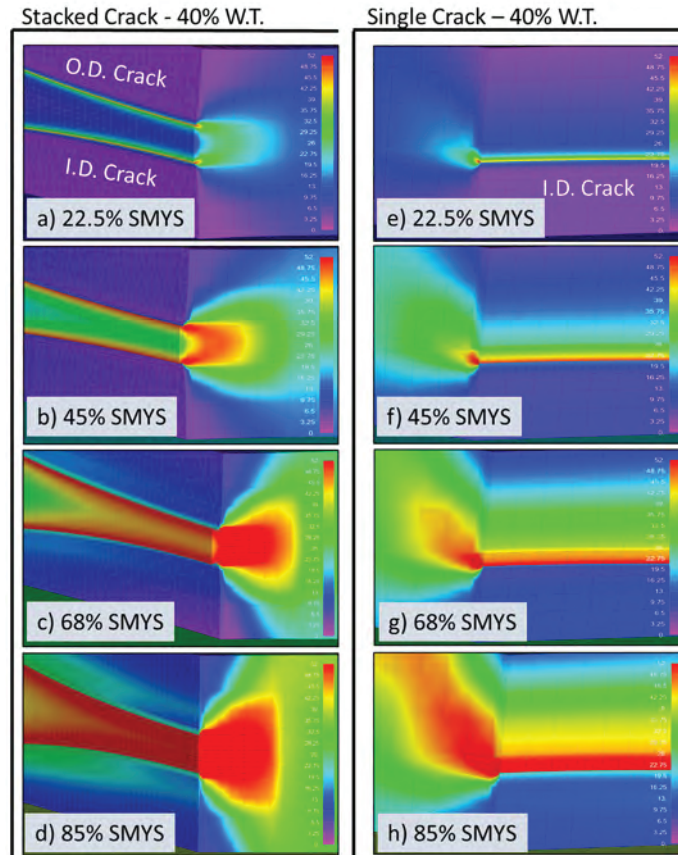
A curve labeled as a combined stack crack is also shown. The combined curve assumes  $a_{ext}$  and  $a_{int}$  are summed to equal 80% of the WT for this example. This is valuable information following a pipeline inspection because it highlights the degree of conservatism involved if the stacked cracks are characterized as a large singular surface crack with a depth equal to the sum of the stacked cracks.



**Figure 4.** Stress intensity versus pressure for a 16-inch (406-mm) OD and 0.28-inch (7.14-mm) WT pipe with equal stacked cracks that measure 40% of the WT.

The stress intensity versus pressure chart in Figure 4 highlights four unique pressure points with dark black circles. These increasing pressure points correspond to the montage of 3-D images shown in Figure 5, which highlight the effect of increasing stress along the crack front and in the ligament prior to yielding. Figure 5 shows the von Mises stress, where the maximum value is set to the yield strength of 52 ksi for this example (the maximum von Mises scale is always set to yield in the following figures). Figure 5a highlights an increase in the stacked cracks ligament stress, while a similar amount of stress is observed near the single ID cracks front in Figure 5e, which corresponds to a similar stress intensity in Figure 4. Figure 5b and Figure 5f are particularly interesting because these images correspond to the internal pressure just slightly past where the stress intensity curves in Figure 5 begin to deviate at 45% SMYS. It is observed at 45% SMYS that the stress in the ligament increased in between the crack fronts, and the ligament is beginning to yield. The beginning of ligament yielding for the stacked crack corresponds to the pressure at which the stacked and singular stress intensity curves deviate from one another in Figure 4.

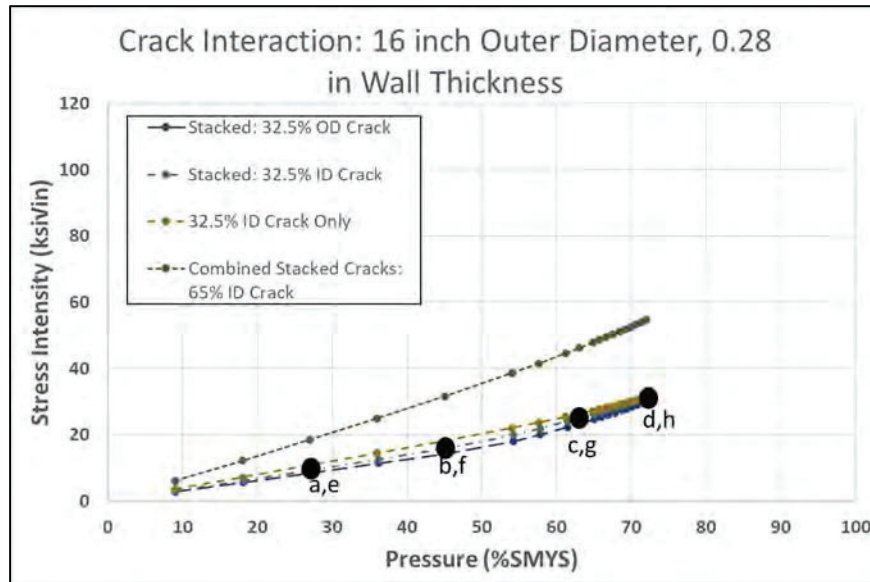
Next, the case in which  $a_{ext}$  and  $a_{int}$  both equal 32.5% of the WT is explored for the same pipe geometry. The chart of stress intensity versus pressure is noticeably different in Figure 6 compared to Figure 5. Here, the stacked cracks behave similarly to the single surface-breaking ID crack, indicating minimal interaction between the stacked cracks. Again, four pressure points are explored, which are highlighted by four black dots in Figure 6. The shallower stacked cracks in Figure 7 compared to Figure 5 demonstrate that ligament yielding occurs at a higher pressure for shallower cracks. Figure 7c and Figure 7d demonstrate the progression of yielding around the ligament, which is achieved at lower pressure for the 40% WT case, as observed in Figure 5b.



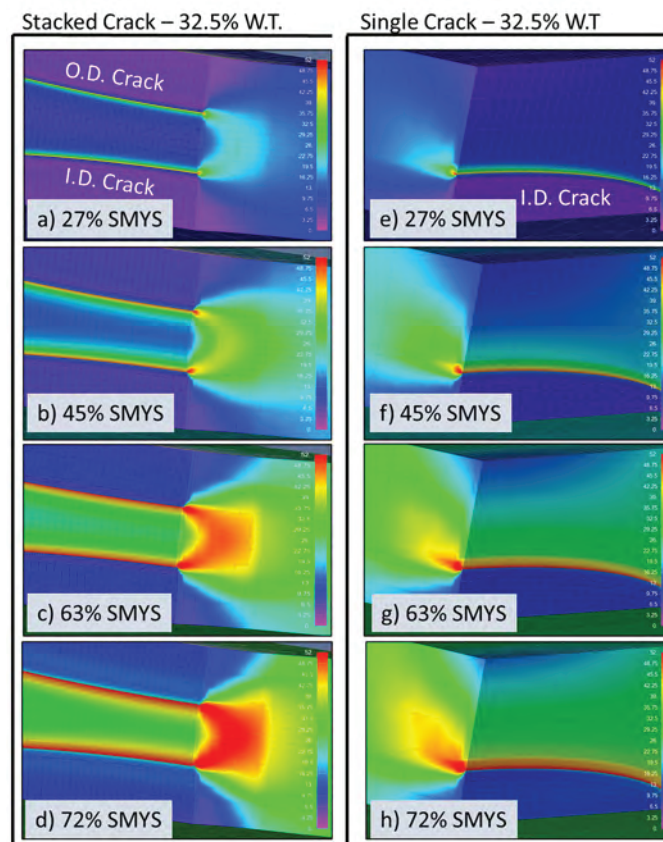
**Figure 5.** A montage of the von Mises stress for equal stacked cracks that measure 40% WT (a through d) and a single ID crack that measures 40% WT (e through h).

The stress intensity curves for the stacked cracks are relatively like the single ID surface-breaking crack in Figure 6. There appear to be the beginnings of a rise in the stress intensity as all the curves begin to converge at 72% of SMYS in Figure 6. Thus, if the simulation was carried out past 72% SMYS in Figure 6, interaction would likely be observed as the ligament completely approaches yield. Because it is unlikely a pipeline would be operated higher than 72% of SMYS, the simulation was not performed past 72% of SMYS.

Figure 6 also plots the stress intensity for a combined stacked crack, which is the summation of  $a_{ext}$  and  $a_{int}$ . This demonstrates the level of conservatism if the stacked cracks are characterized as a singular ID surface-breaking crack.



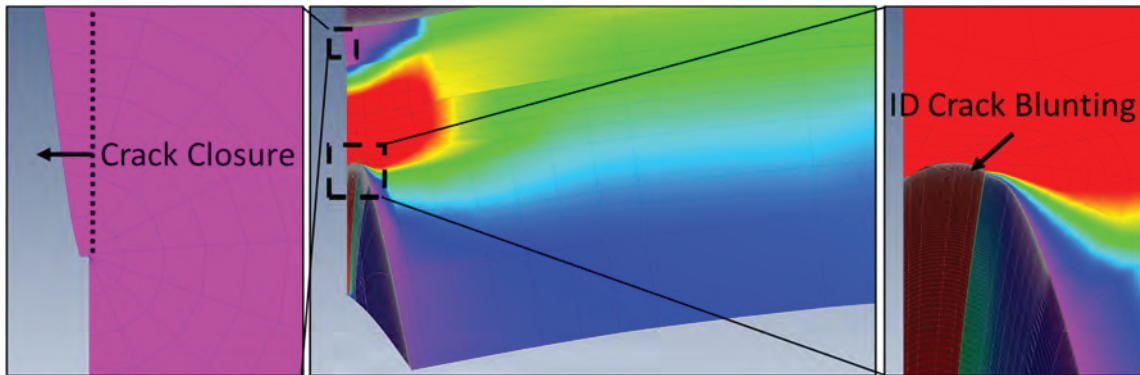
**Figure 6.** Stress intensity versus pressure for a 16-inch (406-mm) OD and 0.28-inch (7.14-mm) WT pipe with equal stacked cracks that measure 32.5% of the WT.



**Figure 7.** A montage of the von Mises stress for equal stacked cracks that measure 32.5% WT (a through d) and a single ID crack that measures 32.5% WT (e through h).

## 4.2 Unequal $a_{\text{ext}}$ and $a_{\text{int}}$ Crack Depths

After exploring equal stacked cracks in Section 4.1, this section investigates stacked cracks in which  $a_{\text{ext}}$  and  $a_{\text{int}}$  have different depths, which is like the unpredictable scenario observed after pipeline inspection is performed. The results in Table 3 demonstrate a combination of depth scenarios and whether they meet the modified API 579 interaction criteria, equation 2. The simulations have shown that the fulfillment of API 579 interaction criteria is not simply “Yes” or “No” because the crack sizes and pipe material dictate the pressure at which crack interaction is initiated. Because the internal crack has crack face pressure, it was decided to maintain it as the deeper of the two cracks for conservatism. The results in Table 3 suggest that when the ligament between the external and internal crack is greater than 27% of the WT, the cracks do not interact below 72% of SMYS, assuming the internal crack is 50% of the WT or less. For the 60%  $a_{\text{int}}$  crack case, interaction is possible at high stresses even though the ligament is greater than 27% of the WT. However, the shallow external crack  $a_{\text{ext}} = 10\%$ , is observed to close, as shown in Figure 8. Thus, the results observed at higher stresses (>40% SMYS) may not be reliable. Additional work would be required to add contact to the models to prevent closure past the symmetry plane, which may alter the results in Table 3 and Table 4 for the  $a_{\text{ext}}/a_{\text{int}} = 10/60$  cases. Since a 60% deep single crack would be dug by most operators it was decided to direct attention towards shallower stacked crack geometry.



**Figure 8.** A stacked crack with  $a_{\text{ext}} = 10\%$  and  $a_{\text{int}} = 60\%$ . Crack closure is observed in the external 10% deep crack (left) while the internal 60% deep crack (right) is blunting. Contact will be added in prevent crack closure in later work.

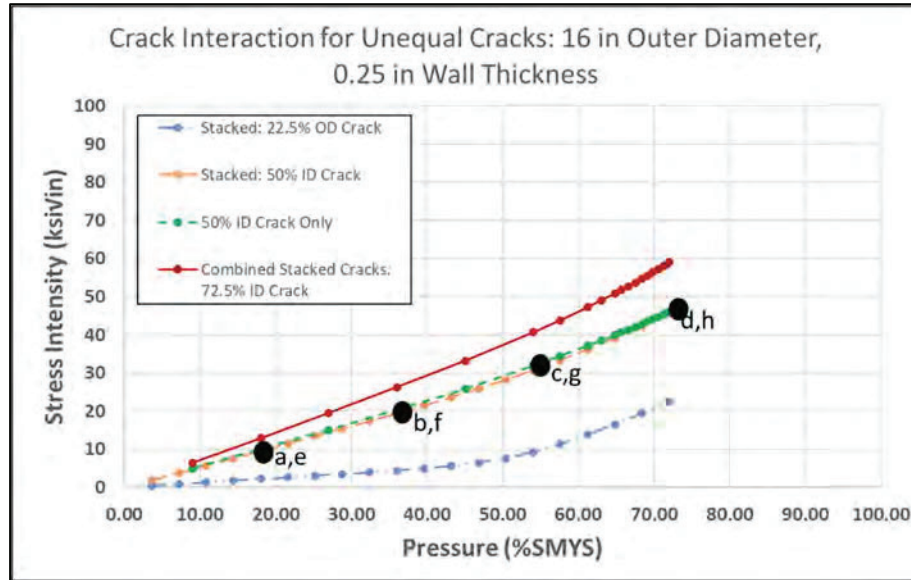
The cracks with  $a_{\text{int}} = 50\%$  of the WT showed no obvious crack interaction at typical operating pressures, as outlined in Table 3. A plot of the stress intensity versus pressure for a pipe with 16-inch (406-mm) OD, 0.25-inch WT, and 22.5%  $a_{\text{ext}}$  is shown in Figure 9. Unlike the equal stacked crack stress intensity profiles shown in Section 4.1, the OD and ID cracks have different stress intensity profiles due to different starting depths. Only the single ID surface crack was simulated for comparison because it is the deepest of the stacked cracks. The simulations were run to 72% of SMYS with no obvious deviation between the single and stacked ID crack in Figure 9. The four black pressure points in Figure 9 are explored with 3-D images in Figure 10. The von Mises stress profiles show very similar levels of yielding at the ligament for the stacked crack compared to the remaining ligament for the single crack. This observation suggests that the external stacked crack does not interact with the internal crack.



**Table 3.** Crack models demonstrate the percentage of SMYS where crack interaction starts when the OD and ID crack depths are not equal. Crack length was  $2c = 2$  inch (50.8 mm).

Pipe OD	Pipe WT	Pipe grade	$a_{ext}/a_{int}$ crack depths	Remaining ligament	Stacked crack interaction begins at?	Meet Modified API crack interaction criteria (eq. 2)
Inch (mm)	Inch (mm)		% WT	%WT	% SMYS	
16 (406)	0.25 (6.35)	X52	30/40	30	65	NO
			35/40	25	50	NO
			40/40	20	40	YES
			20/50	30	>72	NO
			22.5/50	27.5	>72	NO
			25/50	25	>65	YES
			10/60	30	>70	YES
24 (609)	0.281 (7.14)	X52	30/40	30	65	NO
			35/40	25	50	NO
			40/40	20	40	YES
			20/50	30	>72	NO
			22.5/50	27.5	>72	NO
			25/50	25	>65	YES
			10/60	30	>70	YES
12.75 (324)	0.219 (5.56)	X52	30/40	30	65	NO
			35/40	25	50	NO
			40/40	20	40	YES
			20/50	30	>72	NO
			22.5/50	27.5	>72	NO
			25/50	25	>65	YES
			10/60	30	>70	YES
16 (406)	0.314 (8.0)	X46	30/40	30	>72	NO
			35/40	25	55	NO
			40/40	20	45	YES
			20/50	30	>72	NO
			22.5/50	27.5	>72	NO
			25/50	25	>72	YES
			10/60	30	>70	YES





**Figure 9.** Stress intensity versus pressure for a 16-inch (406-mm) OD and 0.25-inch (6.35-mm) WT pipe with unequal stacked cracks that measure  $a_{ext} = 22.5\%$  WT and  $a_{int} = 50\%$  of WT.

As  $a_{ext}$  is slightly increased from 22.5% to 25% of the WT, early signs of crack interaction are observed near 72% of SMYS, where the simulation stopped (Figure 11). However, prior to 72% of SMYS, the results are nearly identical to those shown in Figure 9. The modified API 579 interaction criteria (equation 2) state that the stacked cracks measuring  $a_{ext}/a_{int} = 25\%/50\%$  meet the interaction criteria. However, the simulations show that interaction does not occur unless the internal pressure is relatively high for typical pipeline operations.

Next, stacked cracks with  $a_{int} = 40\%$  of the WT are investigated. In Section 4.1, it was shown that when  $a_{ext}/a_{int} = 40\%/40\%$ , crack interaction occurs at 40% SMYS. When the ligament is increased to 30% of the WT, crack interaction is not observed until approximately 65% of SMYS (Figure 12). Reducing the stacked crack ligament to 25% of WT, which places it between  $a_{ext}/a_{int} = 40\%/40\%$  and  $a_{ext}/a_{int} = 30\%/40\%$  results in crack interaction occurring at approximately 50% of SMYS, as shown in Figure 13. Thus, the remaining ligament plays an important role in the amount of internal pressure required for crack interaction to initiate. The 3-D montage in Figure 14 that corresponds to the stress intensity curves in Figure 13 demonstrates that pressures below 45% SMYS have similar von Mises stresses (Figure 14b and Figure 14f). However, Figure 14c and Figure 14g demonstrate the plastic zone in the stacked crack has grown significantly more than the single crack plastic zone.

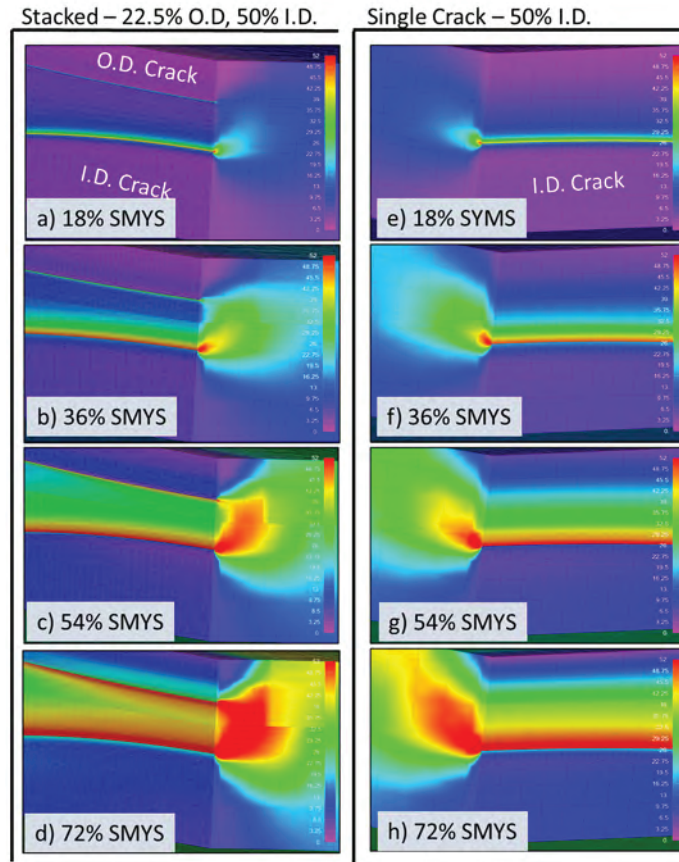


Figure 10. A montage of the von Mises stress for unequal stacked cracks that measure  $a_{ext} = 22.5\%$  WT and  $a_{int} = 50\%$  of WT (a through d) and a single ID crack that measures 50% WT (e through h).

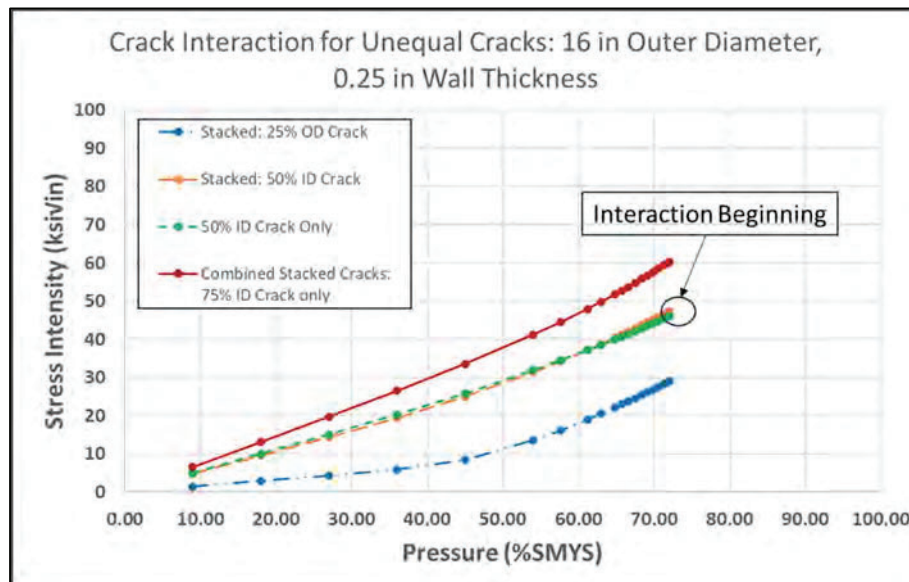


Figure 11. Stress intensity versus pressure for a 16-inch (406-mm) OD and 0.25-inch (6.35-mm) WT pipe with unequal stacked cracks that measure  $a_{ext} = 25\%$  WT and  $a_{int} = 50\%$  WT.

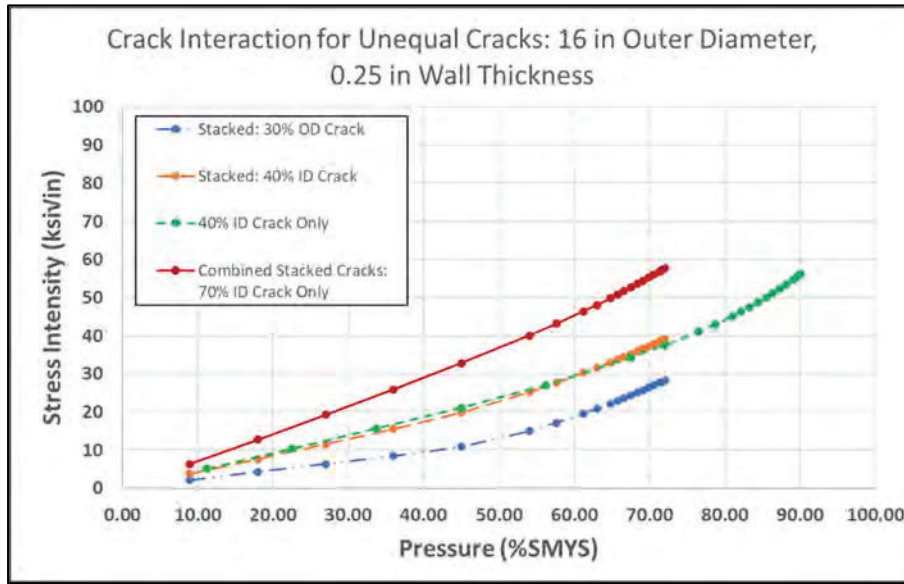


Figure 12. Stress intensity versus pressure for a 16-inch (406-mm) OD and 0.25-inch (6.35-mm) WT pipe with unequal stacked cracks that measure  $a_{ext} = 30\%$  WT and  $a_{int} = 40\%$  WT.

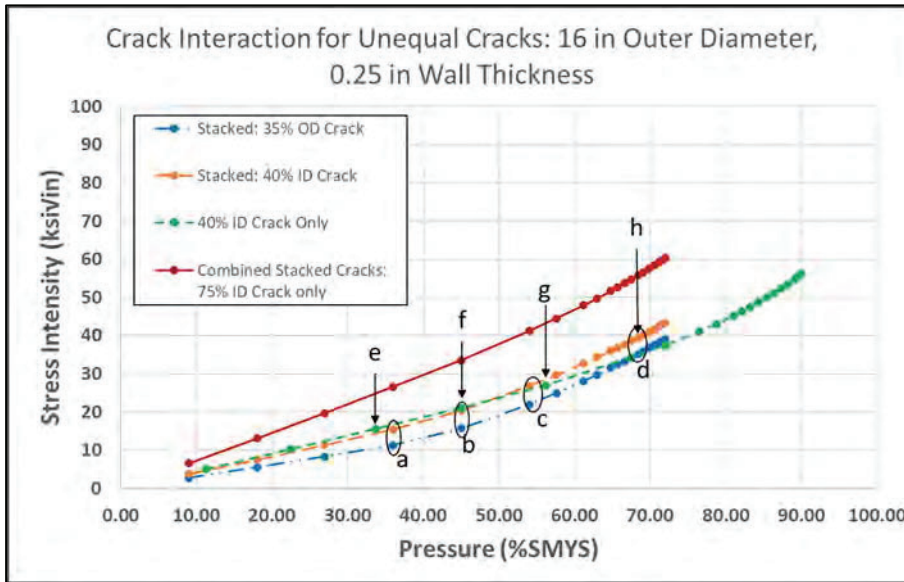
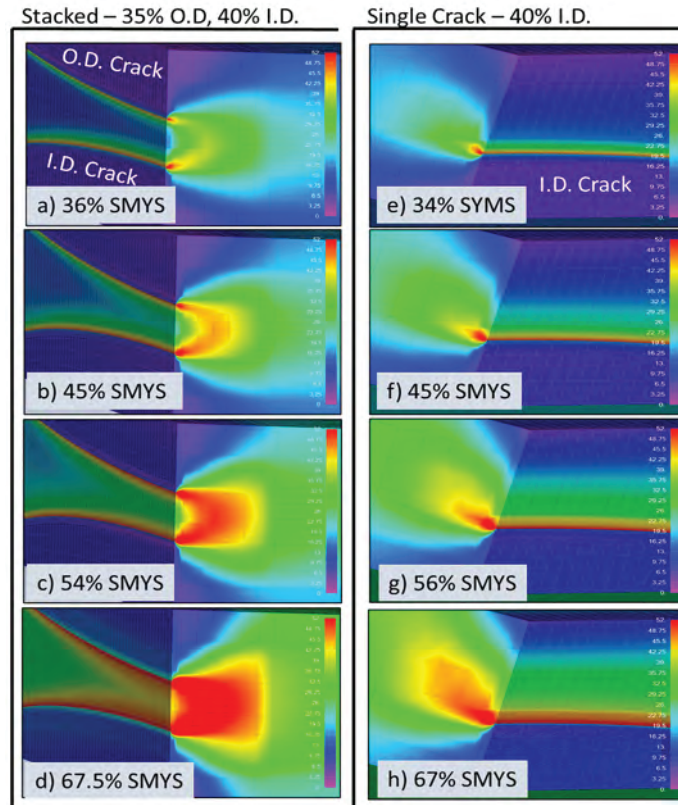


Figure 13. Stress intensity versus pressure for a 16-inch (406-mm) OD and 0.25-inch (6.35-mm) WT pipe with unequal stacked cracks that measure  $a_{ext} = 35\%$  and  $a_{int} = 40\%$  WT.



**Figure 14.** Montage of the von Mises stress for unequal stacked cracks that measure  $a_{\text{ext}} = 35\%$  WT and  $a_{\text{int}} = 40\%$  of WT (a through d), single ID cracks that measures 40% WT (e through h).

### 4.3 Double Length Stacked Cracks ( $2c = 4$ inch [101.6 mm])

Section 4.2 explored unequal stacked cracks while maintaining a constant length of  $2c = 2$  inch (50.8 mm). This section leveraged the same test matrix from Table 3, except increased all crack lengths to  $2c = 4$  inch (101.6 mm). The summarized results in Table 4 demonstrate findings similar to Table 3. However, by doubling the crack lengths, interaction tends to occur slightly earlier. For example, Figure 15 illustrates the interaction in a 16-inch OD pipe with 0.25-inch WT when  $a_{\text{ext}} = 35\%$  and  $a_{\text{int}} = 40\%$  compared to a single crack with  $a_{\text{int}} = 40\%$ . The ID crack curves deviate from one another around 45 to 50% SMYS, indicating that stacked cracks interact.

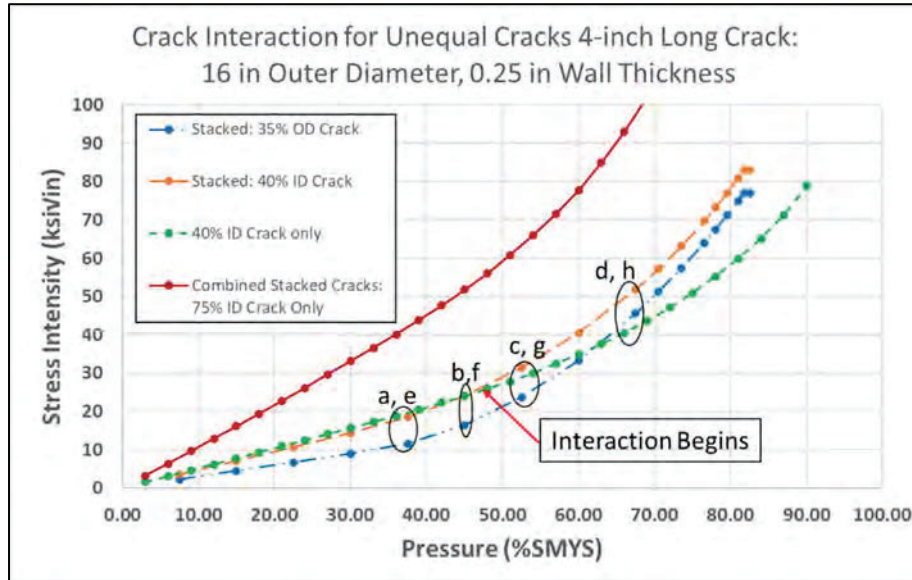
Comparing Figure 15 to Figure 13, similar trends are observed between the crack lengths of  $2c = 4$  inches (101.6 mm) and 2 inch (50.8 mm). The difference is that interaction occurs for the longer crack at approximately 45% SMYS. A montage of the von Mises stress development before and after crack interaction is shown in Figure 16. When this montage is compared to the montage for the 2-inch length cracks in Figure 14, they are nearly identical. The one difference is Figure 16d, which appears to show more plasticity along the entire crack front compared to Figure 14d. When comparing the stress intensity curves in Figure 15 and Figure 13, near 70% of SMYS, the stress intensity value is higher for the 4-inch-long cracks. This difference explains seeing plasticity along the entire crack front. Besides these slight differences, the results for the 4-inch-long crack are very similar to the 2-inch-long cracks.

**Table 4.** Crack models demonstrate the percentage of SMYS where crack interaction starts when the OD and ID crack depths are not equal. All crack lengths are  $2c = 4$  inch (101.6 mm). Highlighted cells are associated with future work.

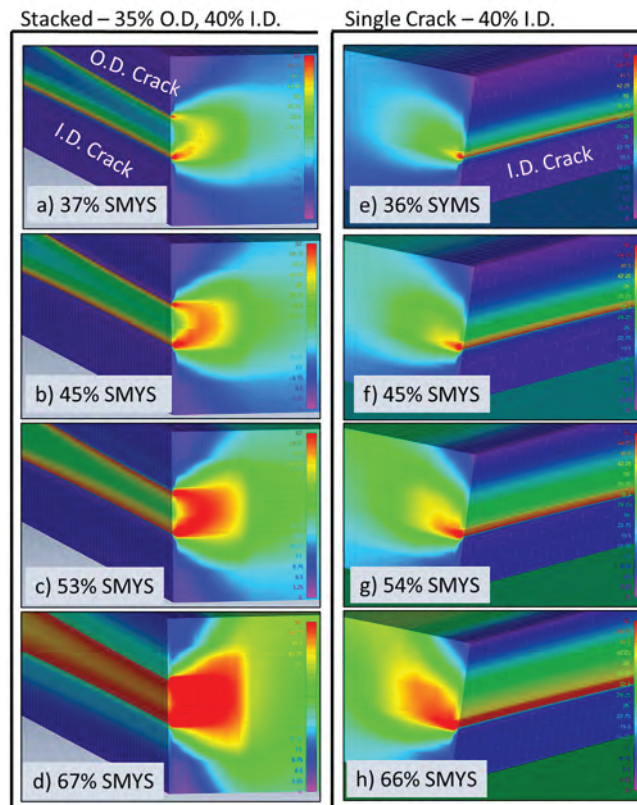
Pipe OD	Pipe WT	Pipe grade	$a_{ext}/a_{int}$ crack depths	Remaining ligament	Stacked crack interaction begins at?	Meet modified API crack interaction criteria (equation 2)
Inch (mm)	Inch (mm)		% WT	%WT	% SMYS	
16 (406)	0.25 (6.35)	X52	30/40	30	55	NO
			35/40	25	45	NO
			40/40	20	40	YES
			20/50	30	No interaction	NO
			22.5/50	27.5	No interaction	NO
			25/50	25	65	YES
			10/60	30	**	YES
24 (609)	0.281 (7.14)	X52	30/40	30	55	NO
			35/40	25	45	NO
			40/40	20	40	YES
			20/50	30	No interaction	NO
			22.5/50	27.5	No interaction	NO
			25/50	25	65	YES
			10/60	30	**	YES
12.75 (324)	0.219 (5.56)	X52	30/40	30	55	NO
			35/40	25	45	NO
			40/40	20	40	YES
			20/50	30	No interaction	NO
			22.5/50	27.5	No interaction	NO
			25/50	25	65	YES
			10/60	30	**	YES
16 (406)	0.314 (8.0)	X46	30/40	30	60	NO
			35/40	25	45	NO
			40/40	20	40	YES
			20/50	30	No interaction	NO
			22.5/50	27.5	No interaction	NO
			25/50	25	65	YES
			10/60	30	**	YES

\*\* Results do not exist to the author's satisfaction given that a 60% deep single crack would typically be dug.





**Figure 15.** Stress intensity versus pressure for a 16-inch (406-mm) OD and 0.25-inch (6.35-mm) WT pipe with unequal stacked cracks that measure  $a_{ext} = 35\%$  and  $a_{int} = 40\%$  WT. Crack lengths were all  $2c = 4$  inch (101.6 mm).



**Figure 16.** Montage of the von Mises stress for unequal stacked cracks that measure  $a_{ext} = 35\%$  WT and  $a_{int} = 40\%$  of WT (a through d), single ID cracks that measures 40% WT (e through h). All cracks have length  $2c = 4$  inch (101.6 mm).

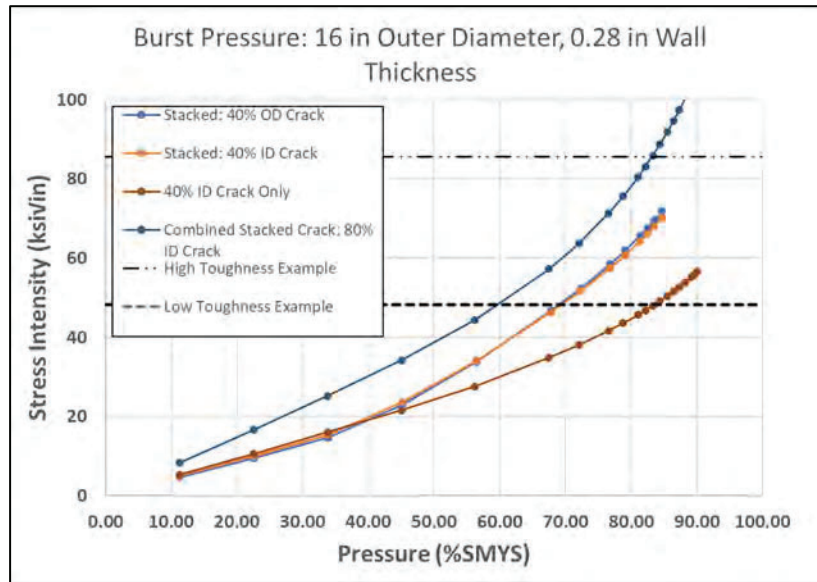


#### 4.4 Burst Pressure

Sections 4.1 to 4.3 explored how the stress intensity curves could identify crack interaction. However, the pipe material fracture toughness can predict burst pressure based upon where it intersects the stress intensity curves. Figure 17 is the same set of curves shown in Figure 4; however, two horizontal lines are introduced that represent assumed fracture toughness values for the pipe material. If fracture toughness specimens are available, the material test values can be used to determine fracture toughness. However, without toughness test data, API 579 can be leveraged to provide conservative and non-conservative fracture toughness for vintage carbon steels. The conservative value of  $K_c = 48.3 \text{ ksi}\sqrt{\text{inch}}$  ( $1678.4 \text{ MPa}\sqrt{\text{mm}}$ ) was determined based on a sulfur content  $>0.01\%$  and assuming the lower 5% on exemption curve B in API 579. The less conservative value of  $K_c = 85.6 \text{ ksi}\sqrt{\text{inch}}$  ( $2974.6 \text{ MPa}\sqrt{\text{mm}}$ ) was derived with the sulfur content being  $\leq 0.01\%$  and the median value of exemption curve B in API 579. This provided a way to bound the results in this example. However, these assumed fracture toughness values are used only to demonstrate how burst pressure is calculated from the stress intensity curves and is not meant to be prescriptive. A recent study [8] that tested a wide range of pre-1980s ERW pipe material could also be leveraged to assign a toughness value to predict the burst pressure for stacked cracks.

If the conservative value of  $K_c = 48.3 \text{ ksi}\sqrt{\text{inch}}$  ( $1678.4 \text{ MPa}\sqrt{\text{mm}}$ ) is assumed for the example shown in Figure 13, the singular crack's burst pressure occurs at approximately 84% SMYS, whereas the stacked crack is shown to have a burst pressure of approximately 70% SMYS. Because the stacked cracks are shown to interact and have a large plastic zone around the ligament, it makes sense for the stacked crack to have a lower burst pressure than the single crack. The combined crack is shown to have the lowest burst pressure at approximately 60% of SMYS, which also makes sense based upon an 80% through-wall, surface-breaking crack. This exemplifies how a pipeline operator could leverage such data to more accurately estimate the burst pressure of a given stacked crack system. Table 5 to Table 7 summarize the burst pressure data for the equal (Table 5) and unequal stacked cracks (Table 6 for  $2c = 2$  inch and Table 7 for  $2c = 4$  inch). "N/A" indicates that, up to the simulated pressure (72% SMYS or greater), the stress intensity curve did not intersect one or two of the assumed fracture toughness values. Simulations would need to be run past 72% or 90% of SMYS to determine their intersection; however, from an operational perspective, it is unlikely for a pipeline system to be operated at higher pressures.

Note, calculated burst pressures are generally more conservative than burst pressures measured in a laboratory environment or in the field [9]. For typical vintage pipe material, this difference can be explained by burst pressure calculations being unable to account for micro-voids in material with elements not specified by the alloy grade, particularly sulfur, which can result in lower and more varied fracture toughness [8] [10], as well as an inability to perfectly size a real-world crack found during inspection amongst other microstructural imperfections [8] [10]. Therefore, burst pressure assessments must leverage conservative fracture databases for vintage steels [8] and assume sizing inaccuracies. Thus, a stacked crack measured in a laboratory could likely produce a higher failure pressure than the numerical results indicate here. However, performing a Level 3, 3-D FE analysis (as was done here) can reduce the conservatism of a Level 2 analysis by more accurately capturing the cracks constraint in a pipeline [8] [11].



**Figure 17.** Stress intensity versus pressure for a 16-inch (406-mm) OD and 0.28-inch (7.14-mm) WT pipe with equal stacked cracks that measure  $a_{ext} = 40\%$  WT and  $a_{int} = 40\%$  of WT. Examples of conservative and medium bound fracture toughness curves are provided, and the intersection with the stress intensity curves represent modelled burst pressures.

**Table 5.** Crack models demonstrate the burst pressure for various equal stacked cracks. St = stacked cracks, s = single crack. All crack lengths equal  $2c = 2$  inch (50.8 mm).

Pipe OD	Pipe WT	Pipe grade	OD and ID crack depths	Burst pressure $Kc = 48.3$ ksiv/inch	Burst pressure $Kc = 85.6$ ksiv/inch
Inch (mm)	Inch (mm)		%	% SMYS	% SMYS
12.75 (324)	0.219 (5.56)	X52	32.5IDst	N/A	N/A
			32.5ODst	N/A	N/A
			32.5IDs	N/A	N/A
			65IDs	65	N/A
			40IDst	70	>90
			40ODst	70	>90
			40IDs	84	N/A
			80IDs	60	80
16 (406)	0.219 (5.56)	X52	32.5IDst	N/A	N/A
			32.5ODst	N/A	N/A
			32.5IDs	N/A	N/A
			65IDs	65	N/A
			40IDst	70	>90
			40ODst	70	>90
			40IDs	84	N/A
			80IDs	58	82
16 (406)	0.25 (6.35)	X52	32.5IDst	N/A	N/A
			32.5ODst	N/A	N/A
			32.5IDs	N/A	N/A
			65IDs	65	N/A
			40IDst	70	90
			40ODst	70	90
			40IDs	84	N/A

Table 5 cont'd

Pipe OD	Pipe WT	Pipe grade	OD and ID crack depths	Burst pressure Kc = 48.3 ksi√inch	Burst pressure Kc = 85.6 ksi√inch
Inch (mm)	Inch (mm)		%	% SMYS	% SMYS
			80IDs	60	84
16 (406)	0.281 (7.14)	X52	32.5IDst	N/A	N/A
			32.5ODst	N/A	N/A
			32.5IDs	N/A	N/A
			65IDs	65	N/A
			40IDst	70	90
			40ODst	70	90
			40IDs	84	N/A
			80IDs	60	84
16 (406)	0.314 (8.0)	X52	32.5IDst	N/A	N/A
			32.5ODst	N/A	N/A
			32.5IDs	N/A	N/A
			65IDs	65	N/A
			40IDst	70	>90
			40ODst	70	>90
			40IDs	84	N/A
			80IDs	60	84
16 (406)	0.314 (8.0)	X46	32.5IDst	N/A	N/A
			32.5ODst	N/A	N/A
			32.5IDs	N/A	N/A
			65IDs	71	N/A
			40IDst	75	>90
			40ODst	75	>90
			40IDs	87	N/A
			80IDs	65	86
24 (609)	0.281 (7.14)	X52	32.5IDst	N/A	N/A
			32.5ODst	N/A	N/A
			32.5IDs	N/A	N/A
			65IDs	65	N/A
			40IDst	70	>90
			40ODst	70	>90
			40IDs	84	N/A
			80IDs	60	85

**Table 6.** Crack models demonstrate the burst pressure for various unequal stacked cracks with  $2c = 2$  inch (50.8 mm).

Pipe OD	Pipe WT	Pipe grade	OD/ ID crack depths	Burst pressure Kc = 48.3 ksi√inch	Burst pressure Kc = 85.6 ksi√inch
Inch (mm)	Inch (mm)		%	% SMYS	% SMYS
16 (406)	0.25 (6.35)	X52	30ODst	N/A	N/A
			40IDst	N/A	N/A
			35ODst	N/A	N/A
			40IDst	N/A	N/A
			40ODst	70	90
			40IDst	70	90
			20ODst	N/A	N/A
			50IDst	N/A	N/A
			22.5ODst	N/A	N/A
			50IDst	N/A	N/A
			25ODst	N/A	N/A
			50IDst	N/A	N/A
			10ODst	N/A	N/A
			60IDst	70	N/A
			40IDs	84	N/A
			50IDs	N/A	N/A
			60IDs	67	N/A
			70IDs	64	N/A
			72.5IDs	62	N/A
			75IDs	62	N/A
80IDs	60	88			
24 (609)	0.281 (7.14)	X52	30ODst	N/A	N/A
			40IDst	N/A	N/A
			35ODst	N/A	N/A
			40IDst	N/A	N/A
			40ODst	70	>90
			40IDst	70	>90
			20ODst	N/A	N/A
			50IDst	N/A	N/A
			22.5ODst	N/A	N/A
			50IDst	N/A	N/A
			25ODst	N/A	N/A
			50IDst	N/A	N/A
			10ODst	N/A	N/A
			60IDst	63	N/A
			40IDs	84	N/A
			50IDs	N/A	N/A
			60IDs	68	N/A
			70IDs	64	N/A
			72.5IDs	64	N/A
			75IDs	63	N/A
80IDs	60	85			
12.75 (324)	0.219 (5.56)	X52	30ODst	N/A	N/A
			40IDst	N/A	N/A
			35ODst	N/A	N/A
			40IDst	N/A	N/A

Table 6 cont'd

Pipe OD	Pipe WT	Pipe grade	OD/ ID crack depths	Burst pressure Kc = 48.3 ksi√inch	Burst pressure Kc = 85.6 ksi√inch
Inch (mm)	Inch (mm)		%	% SMYS	% SMYS
			40ODst	70	90
			40IDst	70	90
			20ODst	N/A	N/A
			50IDst	N/A	N/A
			22.5ODst	N/A	N/A
			50IDst	N/A	N/A
			25ODst	N/A	N/A
			50IDst	N/A	N/A
			10ODst	N/A	N/A
			60IDst	70	N/A
			40IDs	83	N/A
			50IDs	N/A	N/A
			60IDs	67	N/A
			70IDs	62	N/A
			72.5IDs	61	N/A
			75IDs	60	N/A
80IDs	60	84			
16 (406)	0.314 (8.0)	X46	30ODst	N/A	N/A
			40IDst	N/A	N/A
			35ODst	N/A	N/A
			40IDst	N/A	N/A
			40ODst	85	N/A
			40IDst	83	N/A
			20ODst	N/A	N/A
			50IDst	N/A	N/A
			22.5ODst	N/A	N/A
			50IDst	N/A	N/A
			25ODst	N/A	N/A
			50IDst	N/A	N/A
			10ODst	N/A	N/A
			60IDst	N/A	N/A
			40IDs	87	N/A
			50IDs	N/A	N/A
			60IDs	N/A	N/A
			70IDs	70	N/A
72.5IDs	69	N/A			
75IDs	68	N/A			
80IDs	65	86			

**Table 7.** Crack models demonstrate the burst pressure for various unequal stacked cracks with  $2c = 4$  inches (101.6 mm). Highlighted cells are associated with future work.

Pipe OD	Pipe WT	Pipe grade	OD/ ID crack depths	Burst pressure Kc = 48.3 ksi√inch	Burst pressure Kc = 85.6 ksi√inch
Inch (mm)	Inch (mm)		%	% SMYS	% SMYS
16 (406)	0.25 (6.35)	X52	30ODst	80	N/A
			40IDst	70	88
			35ODst	68	N/A
			40IDst	66	N/A
			40ODst	58	74
			40IDst	58	74
			20ODst	N/A	N/A
			50IDst	62	82
			22.5ODst	84	N/A
			50IDst	62	81
			25ODst	75	N/A
			50IDst	60	79
			10ODst	**	**
			60IDst	**	**
			40IDs	74	N/A
			50IDs	60	83
			60IDs	51	73
			70IDs	45	67
			72.5IDs	43	64
			75IDs	43	64
80IDs	40	58			
24 (609)	0.281 (7.14)	X52	30ODst	80	N/A
			40IDst	70	88
			35ODst	68	85
			40IDst	66	83
			40ODst	58	76
			40IDst	58	76
			20ODst	89	N/A
			50IDst	63	84
			22.5ODst	83	N/A
			50IDst	60	83
			25ODst	77	N/A
			50IDst	60	79
			10ODst	**	**
			60IDst	**	**
			40IDs	73	N/A
			50IDs	60	83
			60IDs	51	77
			70IDs	46	70
			72.5IDs	45	68
			75IDs	46	67
80IDs	44	62			
12.75 (324)	0.219 (5.56)	X52	30ODst	80	N/A
			40IDst	70	N/A
			35ODst	70	85
			40IDst	67	77



Table 7 cont'd

Pipe OD	Pipe WT	Pipe grade	OD/ ID crack depths	Burst pressure Kc = 48.3 ksi√inch	Burst pressure Kc = 85.6 ksi√inch
Inch (mm)	Inch (mm)		%	% SMYS	% SMYS
			40ODst	62	76
			40IDst	61	76
			20ODst	86	N/A
			50IDst	62	83
			22.5ODst	N/A	N/A
			50IDst	62	N/A
			25ODst	74	87
			50IDst	62	79
			10ODst	**	**
			60IDst	**	**
			40IDs	73	N/A
			50IDs	60	82
			60IDs	50	72
			70IDs	43	64
			72.5IDs	43	63
			75IDs	41	60
80IDs	40	54			
16 (406)	0.314 (8.0)	X46	30ODst	82	N/A
			40IDst	73	N/A
			35ODst	71	89
			40IDst	69	80
			40ODst	62	80
			40IDst	62	80
			20ODst	N/A	N/A
			50IDst	66	85
			22.5ODst	85	N/A
			50IDst	66	85
			25ODst	79	N/A
			50IDst	65	84
			10ODst	**	**
			60IDst	**	**
			40IDs	76	N/A
			50IDs	65	86
			60IDs	56	80
			70IDs	50	73
72.5IDs	48	70			
75IDs	47	65			
80IDs	49	70			

\*\* Results do not exist to the author's satisfaction given that a 60% deep single crack would typically be dug.

## 5. Model Qualification

A model qualification was performed by comparing burst pressure estimates produced from the FEA models of singular cracks with those produced from the CorLAS™ crack model, accounting for appropriate model error as determined by Zhang et al. [12] and Yan et al. [13]. Zhang et al. explored the model error between predicted burst pressures using CorLAS™ and experimentally measured failure pressures of full-scale pipe burst tests. The model error was calculated as the ratio of experimental failure pressure to that predicted by CorLAS™ and follows a normal distribution with a mean of 1.02 and coefficient of variation (COV) of 13%. In a similar study, Yan et al. also investigated model error, but rather than sourcing experimental burst pressure measurements, their data came from in-service and hydrotest failures, which assumed semi-elliptical crack profiles.

The Yan et al. work provided a model error with a mean of 1.27 and COV of 16%. The data in Table 5 that correspond to singular cracks were interpolated for comparison with the model error determined from Zhang et al. and Yan et al. Unity lines were plotted in Figure 18 as the burst pressure's percentage of SMYS versus burst pressure (%SMYS) calculated from the CorLAS™ crack model. The unity curve was multiplied by  $mean \times (1 \pm COV)$  for the values provided by Zhang et al. (i.e., green dotted curve) and Yan et al. (i.e., blue dotted curve) to represent  $\pm 1$  standard deviation bounds of the CorLAS™ model errors. The singular internal cracks modeled in Table 5 for the lower-bound  $Kc = 48.3 \text{ ksi}\sqrt{\text{inch}}$  ( $1678.4 \text{ MPa}\sqrt{\text{mm}}$ ) are plotted against the unity curve and model error curves in Figure 18.

The FE results from this study mainly fall within the model error bounds that were previously calculated from experimental tests and field results, lending confidence that the burst pressures and corresponding stress intensities from the FEA model are reasonable. Notable is the fact that CorLAS™ is most conservative compared to FEA results for cracks with 80% through-wall depth, which is consistent with Yan et al.'s findings. Figure 19 is like Figure 18, except it highlights the upper-bound  $Kc = 85.6 \text{ ksi}\sqrt{\text{inch}}$  ( $2974.6 \text{ MPa}\sqrt{\text{mm}}$ ) data, which also demonstrate a reasonable fit to the model error.

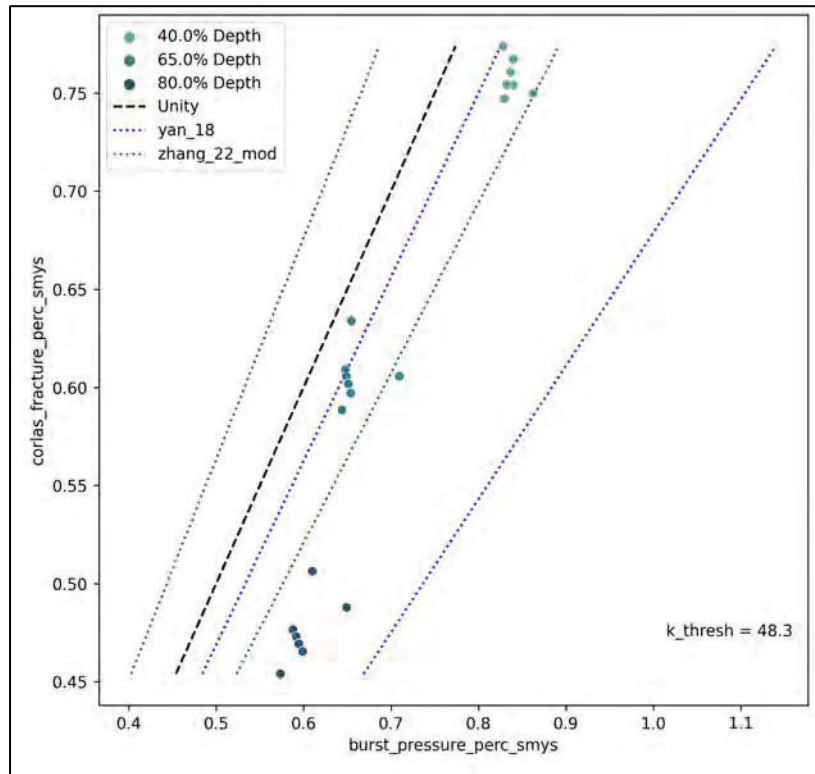


Figure 18. Model error for singular internal cracks assuming  $K_c = 48.3 \text{ ksi}\sqrt{\text{inch}}$  (1678.4  $\text{MPa}\sqrt{\text{mm}}$ ) from Table 5 and Table 6.

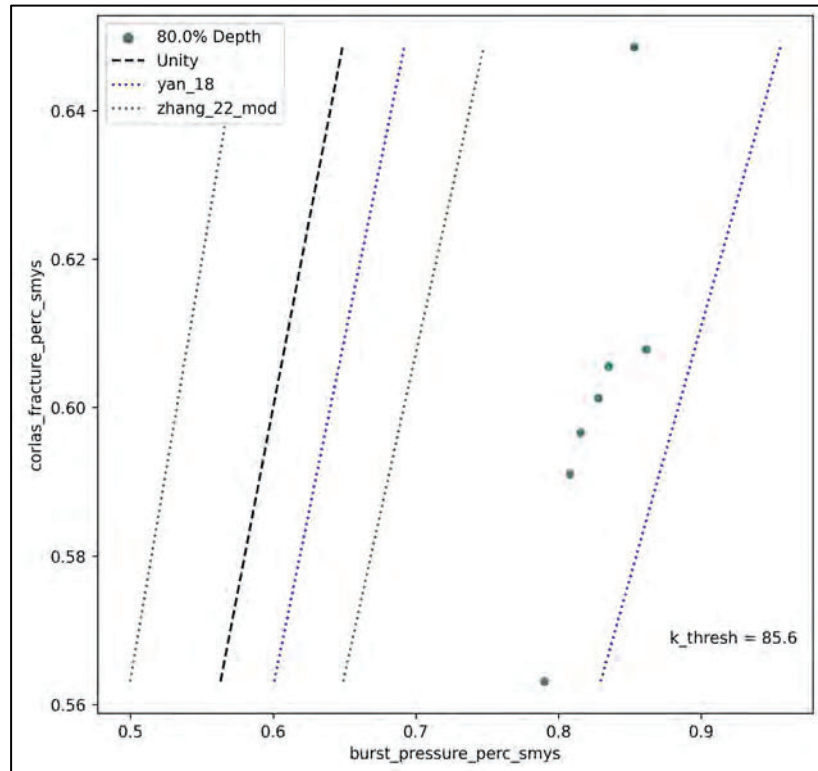


Figure 19. Model error for singular internal cracks assuming  $K_c = 85.6 \text{ ksi}\sqrt{\text{inch}}$  (2974.6  $\text{MPa}\sqrt{\text{mm}}$ ) from Table 5 and Table 6.

## 6. Conclusion

It has been demonstrated that 3-D elastic-plastic FEA models of multiple combinations of stacked crack sizes with various axial orientation, pipe material properties, and operating stress can improve interaction criteria from what are currently found in API 579 Part 9. Equal sized stacked cracks exhibited no interaction up to an internal pressure of 72% of SMYS when the remaining ligament is 35% (equal stacked crack with depths of 32.5% of WT) or greater, but interaction was observed when the remaining ligament is 20% or less. When observed, crack interaction was only prevalent when the pipe's internal pressure reached 45% of SMYS or greater. Unequal stacked cracks are more complex, but in general when the ligament between the external and internal crack is greater than 27% of the WT, the cracks do not interact below 72% of SMYS, assuming the internal crack is 50% of the WT or less. In excess of 50% of WT, interaction is possible at high stresses even when the ligament is greater than 27% of the WT interaction. When the crack lengths are doubled from 2 inches to 4 inches, similar trends were found for unequal cracks, except when interaction is present it tends to occur at a slightly reduced pressures (5 to 10% SMYS).

In addition, the burst capacity of a stacked crack can be calculated from the intersection of the material's fracture toughness along the numerically calculated stress intensity curve. It is valuable to compare the burst capacity of stacked cracks to singular cracks that are the same size as the individual stacked cracks or to a summation of the stacked crack depths. This comparison can help determine the conservatism in decision-making processes.

These improved interaction criteria provide pipeline operators with an easy-to-apply methodology that reduces excess conservatism associated with legacy methods to analyze stacked cracks. In addition, this work has demonstrated the utility of modelling 3-D elastic-plastic FEA models of stacked cracks. Between the numerical model's computational speed and accuracy, the FEA models shown here could be performed following inspection to achieve high-fidelity results.

## 7. References

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